Math 2320 - Final Exam

Name:

1. Let $a(t) = 4\cos(2t) + 8\sin(2t)$ be the acceleration for a particle. Assume we know that the initial position is 5 and the initial velocity is 3. Compute the functions velocity, v(t), and position s(t).

2. Compute the area between the two functions $f(x) = x^2 - 1$ and the line f(x) = 3.

 $3. \int x^3 e^{4x^4 - 1} \, dx$

 $4. \int x^2 e^{3x} \, dx$

5. $\int \cos^2(4x) \, dx$

$$6. \quad \int \frac{1}{x\sqrt{x^2+4}} \, dx$$

7.
$$\int \frac{x+1}{x^2 - 2x - 8} \, dx$$

8. For the following determine if the series converges or diverges. State the test you used, the criteria satisfired your conclusion and as always show your work.

(a)
$$\sum_{n=1}^{\infty} \frac{e^n}{n!}$$

(b)
$$\sum_{n=1}^{\infty} \frac{2n+1}{3n+4}$$
.

(c)
$$\sum_{n=1}^{\infty} (-1)^n \left(1 - \frac{1}{n}\right)^n$$
.

(d)
$$\sum_{n=1}^{\infty} \frac{e^{n^2}}{n!}.$$

9. Compute the Interval of convergence for the following power series.

$$\sum_{n=1}^{\infty} \frac{3}{4n+1} x^n$$

10. Compute the Taylor Series for the function $f(x) = \ln(3x)$ at the point a = 1.