

Show all work for full credit and no calculators or electronic devices allowed.

Name and section: _____

1. Compute the limits

(a) $\lim_{x \rightarrow 3} x^3 + 1$

(b) $\lim_{x \rightarrow 3} \frac{x^2 - x - 6}{x^2 - 9}$

(c) $\lim_{x \rightarrow 1} \frac{x^2}{x^2 - 1}$

(d) $\lim_{x \rightarrow -1} \frac{1}{x + 1}$

(e) $\lim_{x \rightarrow 0} \frac{\sin(x)}{3x}$

(f) $\lim_{x \rightarrow 0} \frac{\sin^2(x)}{x}$

(g) $\lim_{n \rightarrow \infty} \frac{n^3 - 2n + 1}{3n^3 + 5}$

(h) $\lim_{n \rightarrow \infty} \frac{3n + 11}{3n + 11n^2}$

2. Compute the derivative using the **definition** of the derivative

$$f(x) = 3x^2 - x$$

3. Compute the derivative from the formulae.

(a) $f(x) = 3x^2 + 5\sqrt{x} - 3\ln(x)$

(b) $f(x) = \frac{x^3 - 2x + 1}{x}$

(c) $f(x) = 5\sqrt{x}(e^x - 3)$

(d) $f(x) = 7\cos(x)\ln(x)$

(e) $f(x) = (x^3 + 1)^4(3x - 2)^7$

(f) $f(x) = \frac{\sin x}{\cos x}$

Formulae

$$0. \quad \frac{d}{dx} [k] = 0$$

$$1. \quad \frac{d}{dx} [x^n] = nx^{n-1}$$

$$2. \quad \frac{d}{dx} [e^x] = e^x$$

$$3. \quad \frac{d}{dx} [\ln x] = \frac{1}{x}$$

$$4. \quad \frac{d}{dx} [\sin x] = \cos x$$

$$5. \quad \frac{d}{dx} [\cos x] = -\sin x$$

The Power Rule

$$\frac{d}{dx} [(f(x))^n] = n(f(x))^{n-1}f'(x)$$

The Product Rule

$$\frac{d}{dx} [FS] = F'S + FS'$$