## Name:\_

Type up your answers in complete English.

- $11.5: \ \ 46, \ 47, \ 52, \ 55, \ 56$ 
  - 1. Prove Euclid's Lemma: Let a, b and  $c \in \mathbb{Z}$  with  $a \neq 0$ . If a | bc and gcd(a, b) = 1 then a | c.
  - 2. Prove the following: Let b and  $c \in \mathbb{Z}$  and lt p be a prime. If p|bc then p|b or p|c. This is a Corollary to Euclid's Lemma.
  - 3. Prove the following: Let  $c \in \mathbb{Z}$  and lt p be a prime. If  $p|a^2$  then  $p^2|a^2$ . This is a Corollary to Problem 2.