

MATH 5320 Test 1

Name: _____

1. Define the following:

(a) $f : A \rightarrow B$ is **surjective** \iff

(b) M is an **upper bound** for A \iff

(c) $\lim_{n \rightarrow \infty} a_n = \infty$ \iff

(d) $\lim_{x \rightarrow c} f(x) = L$ \iff

2. If (a_n) is convergent then (a_n) is bounded.

3. Show \mathbb{R} is not countable.

4. Do **one** of the following:

- Prove using the $\varepsilon - N$ definition that

$$\lim_{n \rightarrow \infty} \frac{2n + 1}{3n + 1} = \frac{2}{3}$$

- Prove using the $\varepsilon - N$ definition that

$$\lim_{n \rightarrow \infty} \frac{n^2 + 1}{3n + 1} = \infty$$

5. Do **one** of the following:

- If $\lim_{n \rightarrow \infty} a_n = a$ and $\lim_{n \rightarrow \infty} b_n = b$ then show $\lim_{n \rightarrow \infty} a_n b_n = ab$.
- If $\lim_{x \rightarrow c} f(x) = F$ and let $k \in \mathbb{R}$ then show $\lim_{x \rightarrow c} kf(x) = kF$.

6. Prove using the $\varepsilon - \delta$ definition that

$$\lim_{x \rightarrow 2} x^2 + 3x - 5 = 5.$$